

テーラー展開のグラフ : $y = f(x) = e^x$ の場合

$$f(x) = e^x$$

$$f_n(x) = \sum_{k=0}^n \frac{f^{(k)}(0)}{k!} x^k \quad : \quad f(x) \text{ のテーラー展開 (級数) の } x \text{ の べき が } 0 \text{ 乗から } n \text{ 乗までの項の和。}$$

具体的な形は :

$$f_1(x) = 1 + x$$

$$f_2(x) = 1 + x + \frac{1}{2}x^2$$

$$f_3(x) = 1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3$$

$$f_4(x) = 1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4$$

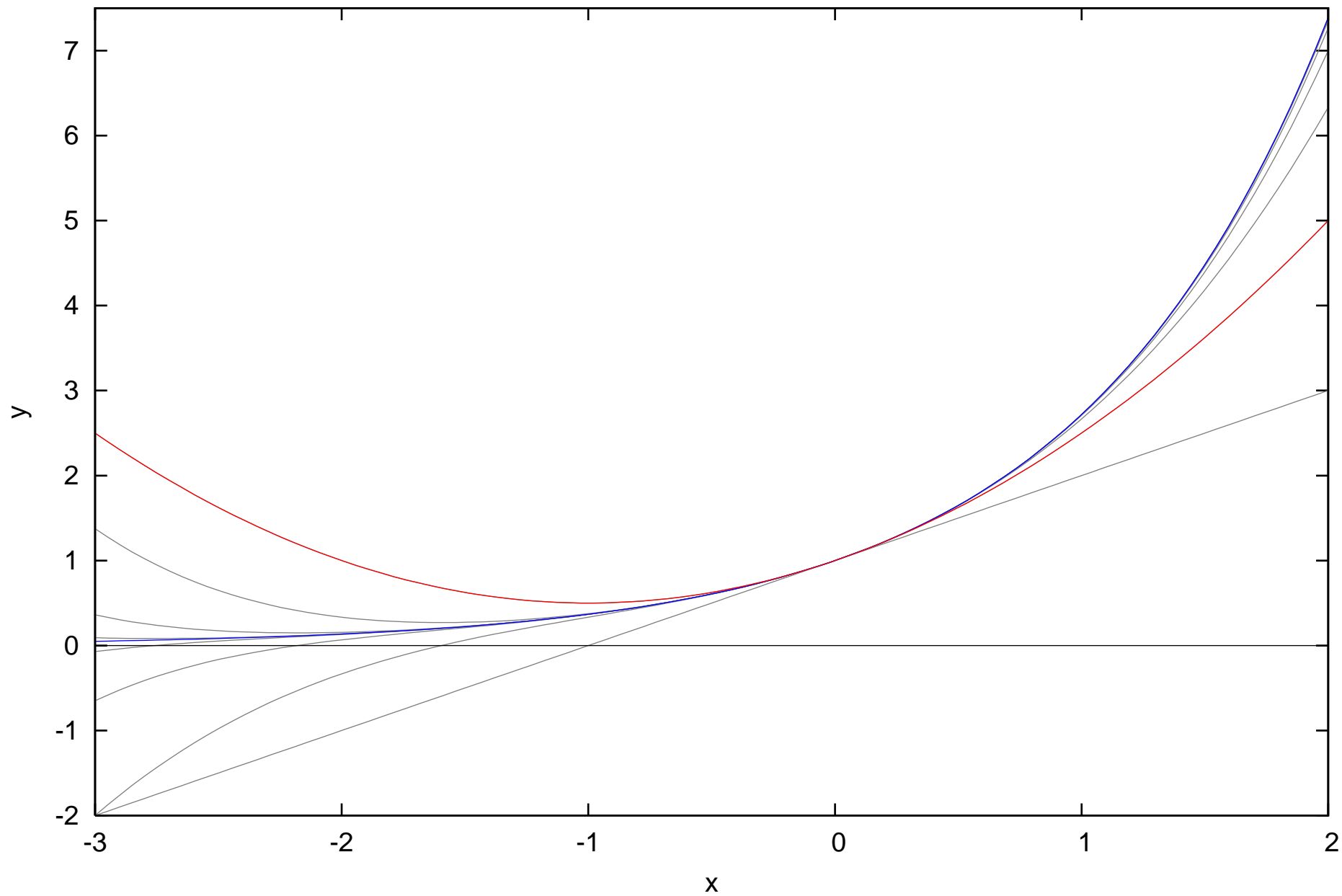
$$f_5(x) = 1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 + \frac{1}{120}x^5$$

$$f_6(x) = 1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 + \frac{1}{120}x^5 + \frac{1}{720}x^6$$

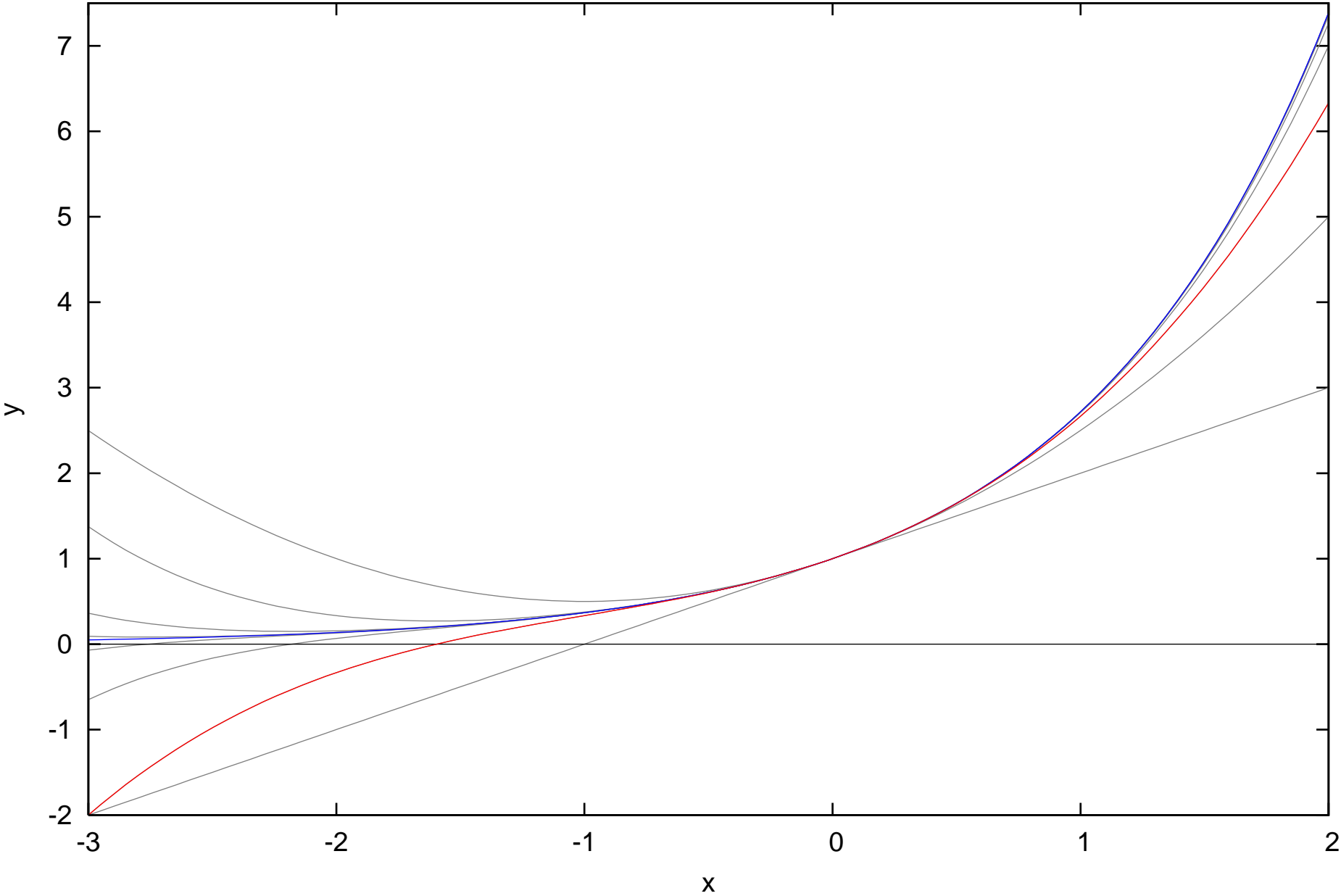
$$f_7(x) = 1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 + \frac{1}{120}x^5 + \frac{1}{720}x^6 + \frac{1}{5040}x^7$$

...

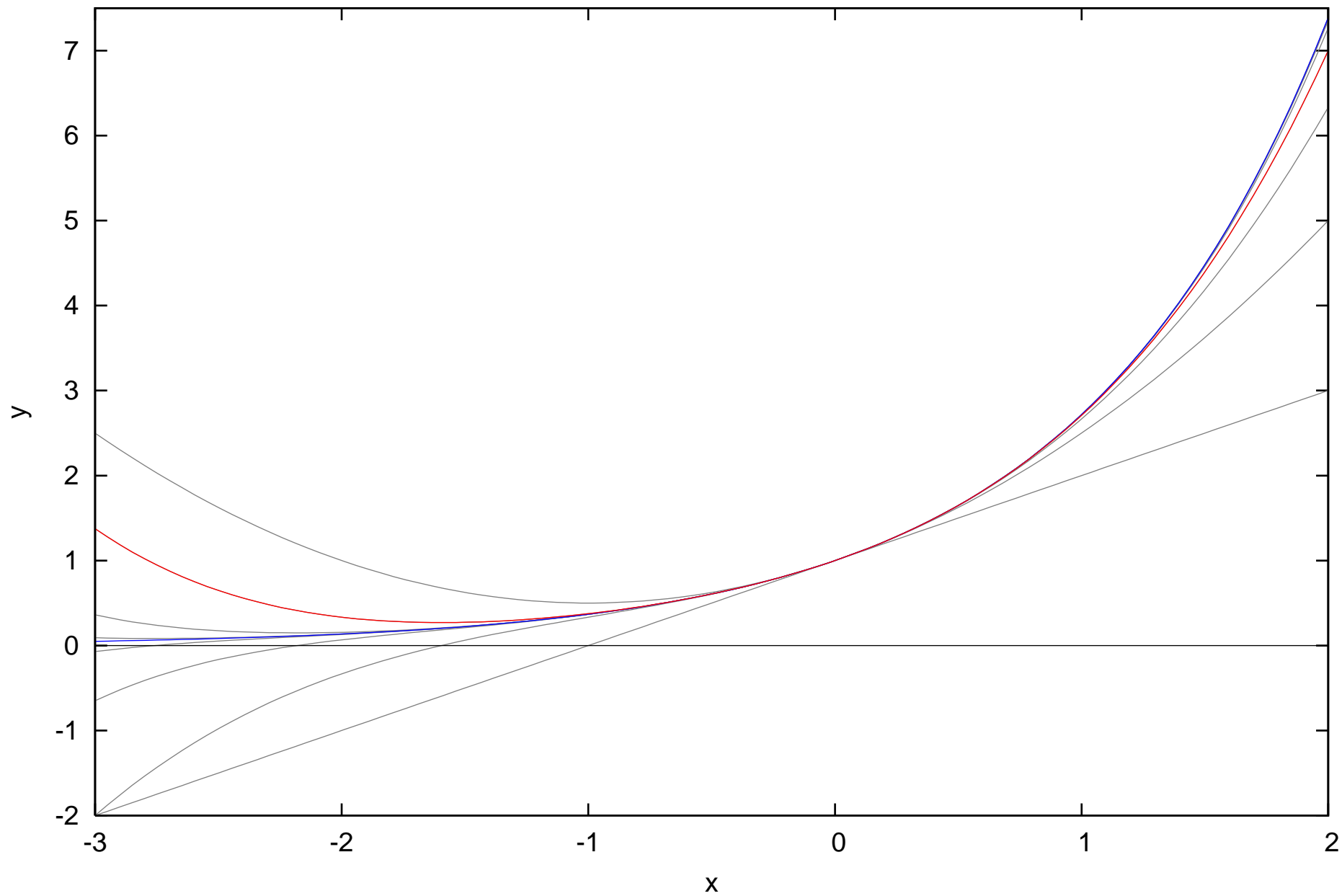
blue curve: $f(x)=\exp(x)$, red curve: $f_2(x)=1+x+x^2/2$



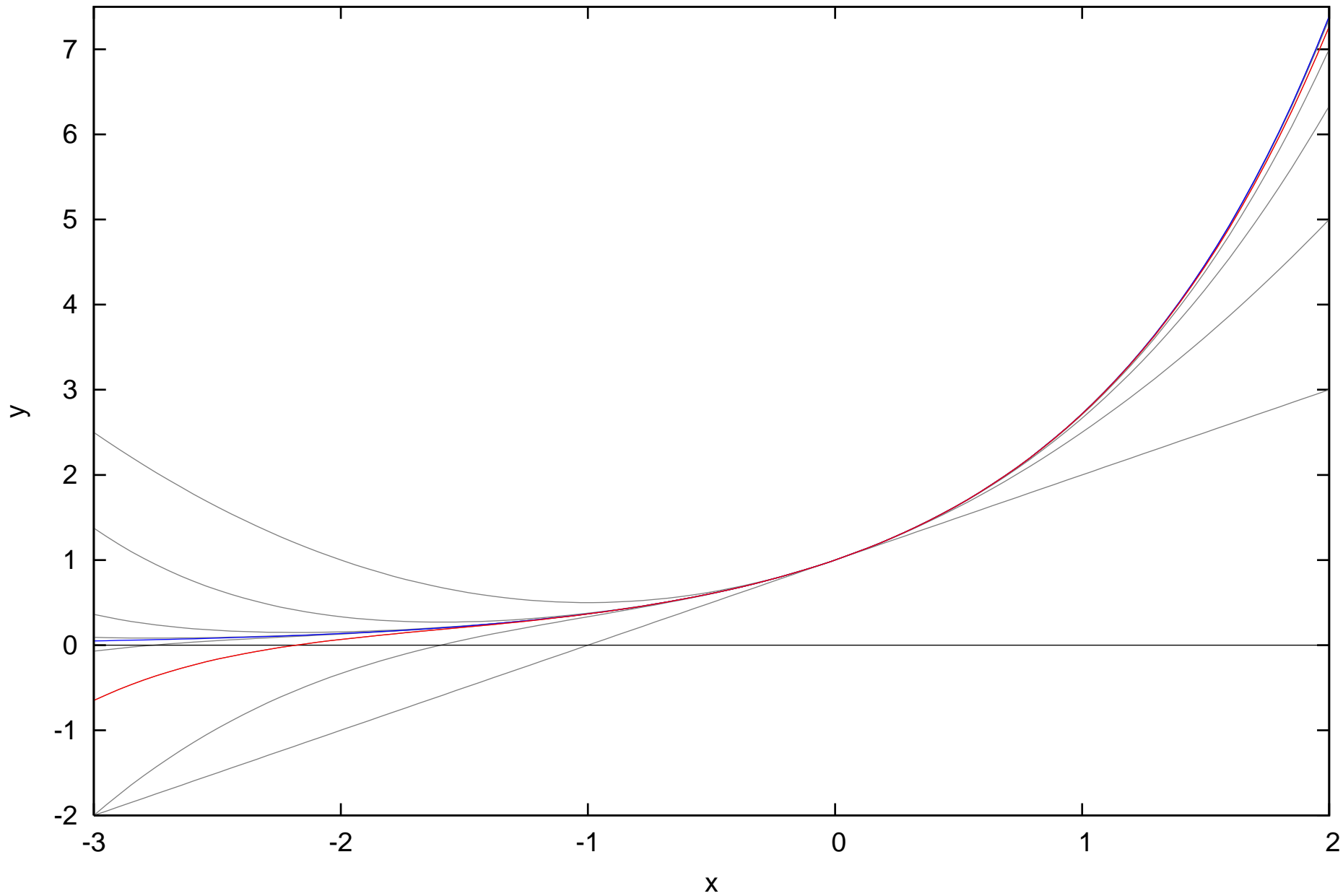
blue curve: $f(x)=\exp(x)$, red curve: $f_3(x)=1+x+x^2/2+x^3/6$



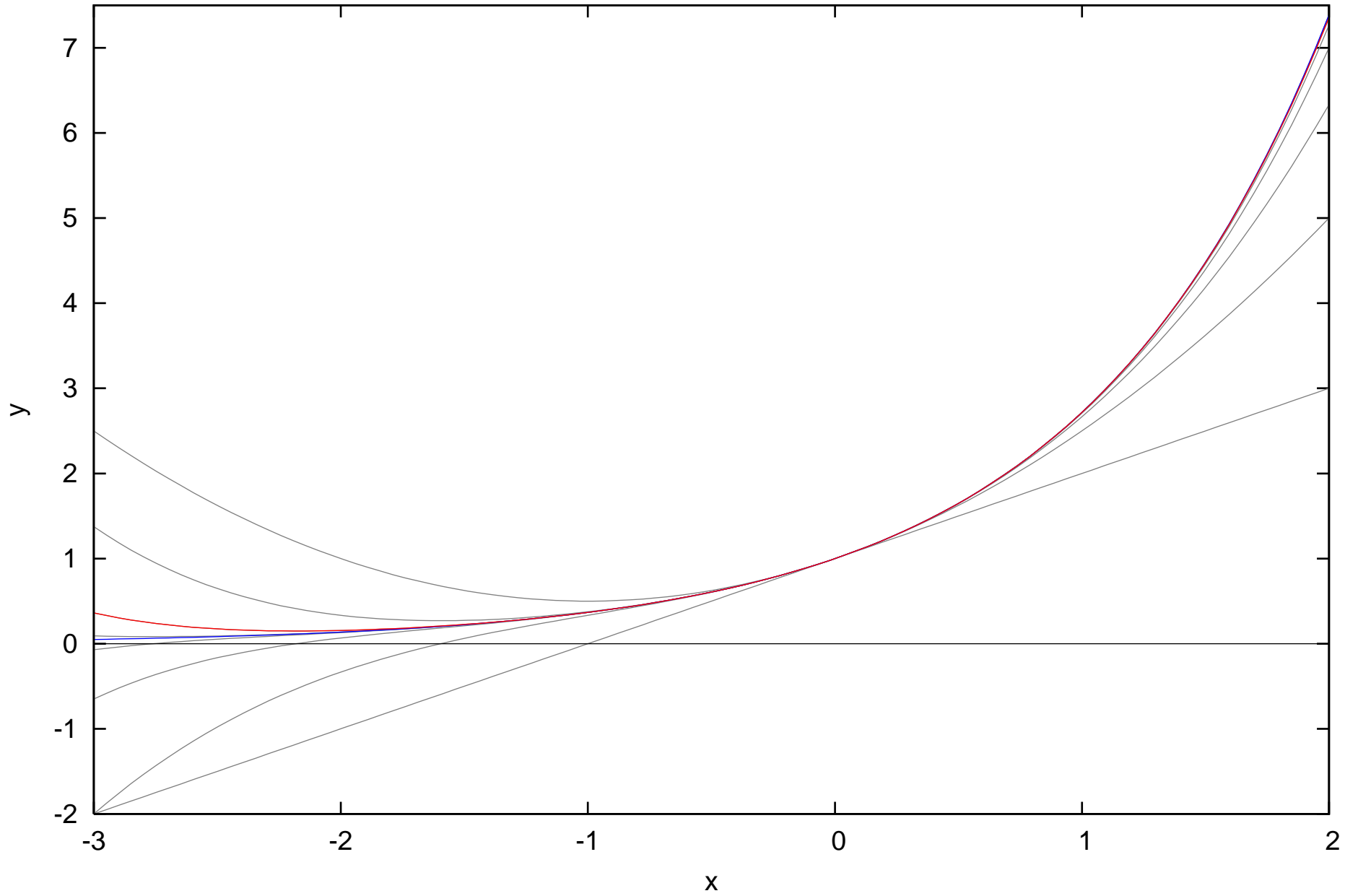
blue curve: $f(x)=\exp(x)$, red curve: $f_4(x)=1+x+\frac{x^2}{2}+\frac{x^3}{6}+\frac{x^4}{24}$



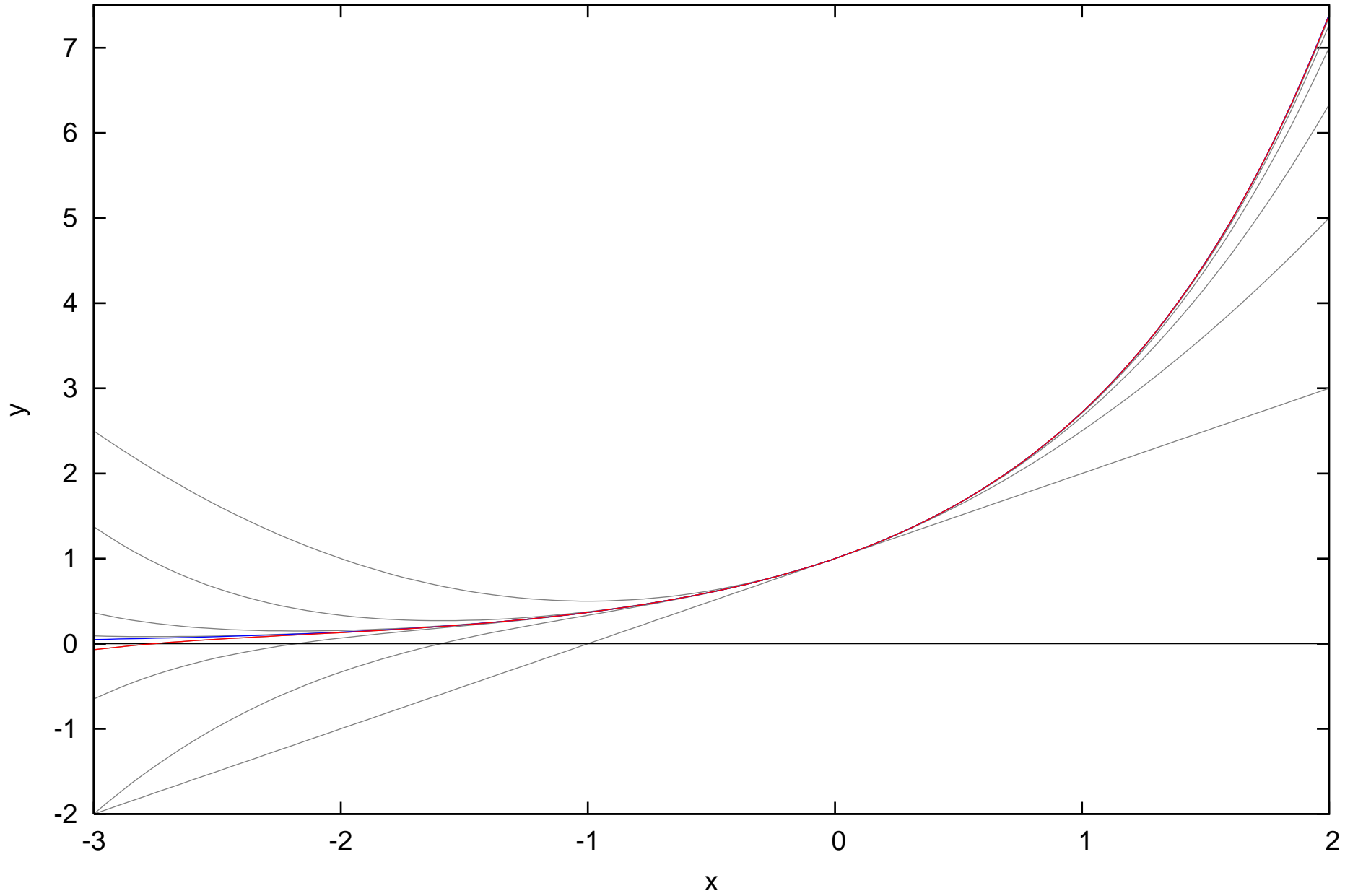
blue curve: $f(x)=\exp(x)$, red curve: $f_5(x)$



blue curve: $f(x)=\exp(x)$, red curve: $f_6(x)$



blue curve: $f(x)=\exp(x)$, red curve: $f_7(x)$



blue curve: $f(x)=\exp(x)$, red curve: $f_8(x)$

